

## CLAIMS

We claim:

- 1      1. A method for analyzing inverse scattering spectral components comprising the steps of:  
2            determining a reflection spectrum of an object of interest;  
3            determining a transmission spectrum of the object;  
4            calculating  $\tilde{V}_1[n]$ ,

5 where  $\tilde{V}_1[n]$  is absolutely and uniformly convergence and is amenable to efficient iterative  
6 computational determination, with leading terms allowing for fast tentative identification of the object  
7 from which the spectrum is obtained.

- 1      2. The method of claim 1, wherein the for  $n = 0$  and/or 1.

- 1      3. The method of claim 2, wherein the  $n = 1$ .

- 1      4. The method of claim 3, wherein

$$\tilde{V}_1(z) = \int_{-\infty}^{+\infty} d(2k)e^{-2ikz} \frac{2i}{k} r_k \left[ 1 + \frac{ik\Delta}{2} \sum_j e^{-ikz_j} V(z_j) \tilde{\psi}_k(z) \right].$$

- 1      5. A method for constructing an acceptable approximation to a true interaction comprising the step  
2 of computing an average according to the following equation:

$$\int_{z_j - \Delta_j/2}^{z_j + \Delta_j/2} dz V_1(z) = \Delta_j V(z_j)$$

4 adapted to obtain n approximate expressions for the  $\Delta_j V(z_j)$  on a sufficiently dense set of points to using  
5 the following equation:

$$V(z) = \sum_j \delta_M(z - z_j | \sigma) V(z_j),$$

7 where the average take into account effects of near-field terms in the Volterra integral equation.

- 1      6. A method for analyzing inverse scattering components of a spectrum of an object of interest,

2 where the method utilizes equations that are absolutely and uniformly convergence and amenable  
3 efficient iterative computational determination, with leading terms allowing for fast tentative  
4 identification of the object from which the spectrum is obtained, where the method comprises the steps  
5 of:

6 obtaining a reflectance and/or transmission spectra of an object of interest using an incident  
7 waveform from the group consisting of an electromagnetic waveform, sonic waveform and mixtures  
8 or combinations thereof;

9 analyzing the spectra using an inverse scattering equations implemented on or in a processing  
10 unit (digital or analog) to derive a potential function  $\tilde{V}_1[n]$  representing the object,

11 where an adequate potential function  $\tilde{V}_1[n]$  is derivable from first few leading terms of the iterative  
12 solution of the equations.

1 7. The method of claim 1, wherein the first few terms comprise the first four terms.

1 8. The method of claim 1, wherein the first few terms comprise the first three terms.

1 9. The method of claim 1, wherein the first few terms comprise the first two terms.

1 10. An analytical instrument including an excitation source for producing an incident waveform,  
2 a detector for receiving either a transmission spectrum or a reflectance spectrum or both a transmission  
3 spectrum and a reflectance spectrum of an object or volume of interest, and a processing unit for  
4 analyzing the spectra, where the processing unit includes software encoding the inverse scattering  
5 method of Claims 1-9.

1 11. A sonic analytical instrument including a sonic excitation source for producing an incident  
2 sonic waveform, a detector for receiving either a sonic transmission spectrum or a sonic reflectance  
3 spectrum or both a sonic transmission spectrum and a sonic reflectance spectrum of an object or  
4 volume of interest, and a processing unit for analyzing the sonic spectra, where the processing unit  
5 includes software encoding the inverse scattering method of Claims 1-9.

1 12. An electromagnetic analytical instrument including an electromagnetic excitation source for

2 producing an incident electromagnetic waveform, a detector for receiving either an electromagnetic  
3 transmission spectrum or an electromagnetic reflectance spectrum or both an electromagnetic  
4 transmission spectrum and an electromagnetic reflectance spectrum of an object or volume of interest,  
5 and a processing unit for analyzing the electromagnetic spectra, where the processing unit includes  
6 software encoding the inverse scattering method of claims 1-9.

1 13. An analytical instrument including a sonic excitation source and an electromagnetic excitation  
2 source for producing an incident sonic waveform and an incident electromagnetic waveform, a detector  
3 for receiving either a sonic transmission spectrum or a sonic reflectance spectrum or both a sonic  
4 transmission spectrum and a sonic reflectance spectrum of an object or volume of interest, a detector  
5 for receiving either an electromagnetic transmission spectrum or an electromagnetic reflectance  
6 spectrum or both an electromagnetic transmission spectrum and an electromagnetic reflectance  
7 spectrum of an object or volume of interest, and a processing unit for analyzing the sonic and  
8 electromagnetic spectra, where the processing unit includes software encoding the inverse scattering  
9 method of Claims 1-9.